

## Nonlinear optical properties of metal/metal free porphyrins and their graphene oxide composites in picosecond regime

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**Abstract.** The nonlinear optical properties of porphyrins (Cu porphyrin, Zn porphyrin and H<sub>2</sub>MHTP) and their covalently linked composites with graphene oxide (GO) have been studied by numerically solving the rate equations and field intensity equation with an iterative predictor-corrector finite-difference time-domain technique. The three-level scheme is introduced to illustrate the interaction between the molecules and laser in picosecond time domain. The optical limiting and dynamical two-photon absorption are investigated. Our numerical results show that GO-porphyrin composites show enhanced nonlinear absorption properties compared with individual porphyrin molecules due to the strong electron acceptor capability of the GO moiety, which agrees with the experimental measurements. Moreover, the dependence of the thickness of the absorber and the pulse duration on the two-photon absorption cross sections of the medium are discussed, indicating that one can modulate the dynamical two-photon absorption process by regulating the parameters of the medium and the laser.

### 1. Introduction

As a newly appeared material, graphene has exhibited remarkable nonlinear optical (NLO) properties, which makes it attracting enormous scientific attention for the potential applications in photonic and optoelectronic fields such as in data storage, optical limiting (OL) etc. [1-4]. Traced back to the most beginning, Wang et al. firstly reported the broadband NLO and OL properties of graphene dispersions with nanosecond pulses at wavelength of 532 and 1064 nm [5]. Their measurements show that nonlinear scattering (NLS), originating from the thermally induced solvent bubbles and microplasmas, are responsible for this nonlinear response. In addition, Liu et al. studied the NLO properties of graphene oxide (GO) with good solubility in nanosecond and picosecond regimes at 532 nm [6], showing that two-photon absorption (TPA) dominated the nonlinear absorption in picosecond regime, while excited state absorption (ESA) plays an important role in nanosecond regime. To further modify the NLO properties of graphene, the covalent or non-covalent functionalization of GO with fullerenes [7], porphyrin [8], oligothiophene [9,10], Fe<sub>3</sub>O<sub>4</sub> nanoparticles [11], and phthalocyanine [12] have been synthesized and studied. These functionalized GO hybrid materials exhibit good NLO behaviors with high NLO absorption coefficients in nanosecond and femtosecond timescale regimes due to the successful formation of donor-acceptor system and the combination of different NLO mechanisms.

It has been shown that porphyrins have many potential applications in optoelectronics, nonlinear optics [13]. Furthermore, metal substituted porphyrins have shown better third order NLO properties than metal free porphyrins [14-16]. Recently, a series of novel covalent GO with different metal

or metal free porphyrins were synthesized experimentally and their NLO properties were explored in picosecond regime [17,18]. However, there is rare theoretical study on the optical properties of graphene or its porphyrin composite. This phenomenon mainly attribute to two reasons: firstly, the limitation of the computational capacity makes theoretical calculation for these complicated systems on the ab-initio level really difficult; secondly, NLO properties of graphene oxide-porphyrin composite depend strongly on the dynamical parameters of the interaction between laser field and the medium.

In this paper, we present a dynamical theory of the sequential TPA for laser pulses and theoretically study the enhanced NLO and OL properties in metal or metal free porphyrins (Cu porphyrin, Zn porphyrin and H<sub>2</sub>MHTP) and their covalently functionalized GO-porphyrin composites (GO-Cu porphyrin, GO-Zn porphyrin and GO-H<sub>2</sub>MHTP) with an iterative predictor-corrector finite-difference time-domain (FDTD) technique by numerically solving the rate equation-field intensity equation. Our numerical results show that all the compounds exhibit outstanding OL performance, which will be useful for sensors or human eye protection and stabilization of light sources for optical communications. In addition, GO-porphyrin composites show enhanced nonlinear absorption properties compared with individual porphyrin molecules, and GO-metal porphyrins show more obvious nonlinear absorption properties compared with GO-metal free porphyrins in picosecond time scales.

### 2. Theoretical methods

As is referred to Ref. [19,20], we have reduced the studied compounds to a simplified model of three-level system: the ground state  $S_0$ , the first excited state  $S_1$  and the higher excited state  $S_2$  due to the good overlap and energy transfer between the energy levels of the porphyrins and the GO. This scheme

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has taken into account two sequential TPA channels  $S_0$  to  $S_1$  and  $S_1$  to  $S_2$ , as shown in Figure 2.1(b).

### 2.1. Rate equations for a three-level system

The populations of  $S_0$ ,  $S_1$ ,  $S_2$  states for a three-level system obey the generalized rate equations:

$$\begin{aligned} \frac{\partial}{\partial t} \rho_{S_0} &= -\gamma_{S_0S_1}(\rho_{S_0} - \rho_{S_1}) - \gamma_{S_0S_2}(\rho_{S_0} - \rho_{S_2}) + \Gamma_{S_1} \rho_{S_1}, \\ \frac{\partial}{\partial t} \rho_{S_1} &= \gamma_{S_0S_1}(\rho_{S_0} - \rho_{S_1}) - \gamma_{S_1S_2}(\rho_{S_1} - \rho_{S_2}) - \Gamma_{S_1} \rho_{S_1} + \Gamma_{S_2} \rho_{S_2}, \\ \frac{\partial}{\partial t} \rho_{S_2} &= \gamma_{S_0S_2}(\rho_{S_0} - \rho_{S_2}) + \gamma_{S_1S_2}(\rho_{S_1} - \rho_{S_2}) - \Gamma_{S_2} \rho_{S_2}, \end{aligned} \quad (1)$$

Where  $\Gamma_{S_0}$ ,  $\Gamma_{S_1}$ ,  $\Gamma_{S_2}$ , are the decay rates of the states  $S_0$ ,  $S_1$ ,  $S_2$  respectively. The total populations are normalized to one:

$$\sum_{n=0}^2 \rho_{S_n} = 1. \quad (2)$$

It is convenient to express one-photon induced transitions (form  $S_0$  to  $S_1$  and form  $S_1$  to  $S_n$ ) rates  $\gamma_{S_0S_1}$  and  $\gamma_{S_1S_2}$  through the transition dipole moments  $d_{S_0S_1}$ ,  $d_{S_1S_2}$  or the corresponding one-photon absorption (OPA) cross section  $\sigma_{S_0S_1}$ ,  $\sigma_{S_1S_2}$ , under rotating wave approximation (RWA).

$$\begin{aligned} \gamma_{S_0S_1}(t) &= \frac{|d_{S_0S_1}|^2 I(t)}{\hbar^2 c \epsilon_0} \frac{\Gamma}{\Omega_{S_0S_1}^2 + \Gamma^2} = \frac{\sigma_{S_0S_1} I(t)}{\hbar \omega} \frac{\Gamma^2}{\Omega_{S_0S_1}^2 + \Gamma^2}, \\ \gamma_{S_1S_2}(t) &= \frac{|d_{S_1S_2}|^2 I(t)}{\hbar^2 c \epsilon_0} \frac{\Gamma}{\Omega_{S_1S_2}^2 + \Gamma^2} = \frac{\sigma_{S_1S_2} I(t)}{\hbar \omega} \frac{\Gamma^2}{\Omega_{S_1S_2}^2 + \Gamma^2}, \\ \Omega_{S_0S_1} &= \omega - \omega_{S_0S_1}, \quad \Omega_{S_1S_2} = \omega - \omega_{S_1S_2}, \end{aligned} \quad (3)$$

Where  $\omega$  is the input light frequency,  $I(t)$  is the instantaneous intensity of the field, and  $\Gamma$  is the homogeneous broadening of the spectral line. We assume  $\hbar\Gamma_{mn} = \hbar\Gamma = 0.1eV$  for all transitions.  $\Omega_{S_0S_1}$  and  $\Omega_{S_1S_2}$  are the detuning of light frequency from resonant frequency.

Similarly, the rate  $\gamma_{S_0S_2}$  of two-photon induced transition from  $S_0$  to  $S_2$  is defined through the TPA cross section  $\sigma_{S_0S_2}$  as follows:

$$\gamma_{S_0S_2} = \frac{\sigma_{S_0S_2} I^2(t)}{2\hbar\omega} \frac{\Gamma^2}{(2\omega - \omega_{S_0S_2})^2 + \Gamma^2}, \quad (4)$$

### 2.2. Field intensity equation

In the case of the picosecond pulse propagating along the  $z$  axis through thin media, where the role of self-focusing and defocusing is small, the change of the refraction and the transverse of the field can thus be neglected. The absorption of the field can be described by field intensity equation:

$$\left(\frac{\partial}{\partial z} + \frac{1}{c} \frac{\partial}{\partial t}\right) I(t) = -N[\sigma^{(1)} I(t) + \sigma^{(2)} I^2(t)]. \quad (5)$$

For our studied system, the total OPA cross section  $\sigma^{(1)}$  and TPA cross section  $\sigma^{(2)}$  are expressed as:

$$\sigma^{(1)} = \sigma_{S_0S_1}(\rho_{S_0} - \rho_{S_1}) + \sigma_{S_1S_2}(\rho_{S_1} - \rho_{S_2}), \quad \sigma^{(2)} = \sigma_{S_0S_2}(\rho_{S_0} - \rho_{S_2}). \quad (6)$$

### 2.3. Calculation of the dynamical TPA cross section

When regardless of significant recombination, diffuse and thermal runaway, the differential equation of the field intensity can be expressed as [21],

$$dI/dz + \alpha I + \beta I^2 = 0, \quad (7)$$

Where  $\alpha$  denotes the linear absorption coefficient and  $\beta$  is the TPA coefficient. The analytical solution can be reformed as follows:

$$1/T(z) = I_0/I(z) = \exp(\alpha z) + [\exp(\alpha z) - 1] \beta I_0 / \alpha, \quad (8)$$

here  $T(z)$  is the transmission of the field intensity at the propagation distance  $z$ .

As to a strong input electric field, the TPA coefficient depends strongly on the input intensity  $I_0$  [22]:

$$\beta = \beta_0 - \xi I_0, \quad (9)$$

Where  $\beta_0$  is the steady-state TPA coefficient and  $\xi$  is a constant. Plug equation (9) into (8), one can notice the inverse transmission  $1/T(z)$  is a quadratic function of the input field intensity  $I_0$ ,

$$\frac{1}{T(z)} = \frac{I_0}{I(z)} = \exp(\alpha z) + \frac{[\exp(\alpha z) - 1] \beta_0}{\alpha} I_0 - \frac{[\exp(\alpha z) - 1] \xi}{\alpha} I_0^2. \quad (10)$$

By fitting equation (10) properly, the absorption coefficients  $\alpha$  and  $\beta_0$  can be determined. The relationships between molecular TPA cross section  $\sigma_{tp}$  and  $\beta_0$  can thus be expressed as below:

$$h\nu\beta_0 = \sigma_{tp} N, \quad (11)$$

where  $h\nu$  is the incident photon energy,  $N$  is the molecular density.

### 2.4. Computational details

Here we investigate the OL behaviors of three different porphyrins (Zn porphyrin, Cu porphyrin, H<sub>2</sub>MHTP) and covalently functionalized GO- (Zn porphyrin, Cu porphyrin, H<sub>2</sub>MHTP) composites. Their structures are shown in Figure 2.1(a). To perform numerical simulations, the resonant transition energies, OPA cross sections, and relaxation rates, TPA coefficient of these compounds are extracted from the experiments [8,17,23]. The corresponding values are collected in Table 2-1. Unfortunately, the TPA cross section  $\sigma_{S_0S_2}$  is not available in the literatures. Thus we determined the values of  $\sigma_{S_0S_2}$  through the relationship in equation (11). In order to save the computation time, the simulations are performed for relatively high concentration and short distance compared with experimental conditions. Fortunately, the numerical results can be compared with the measurements according to the scaling relation  $N_{\text{theo}} L_{\text{theo}} = N_{\text{exp}} L_{\text{exp}}$  where  $L_{\text{theo}} = 0.48$  mm,  $L_{\text{exp}} = 1.0$  cm. Using the above scaling relation, we get the simulation concentrations  $N_{\text{theo}}$  as  $6.33 \times 10^{23}/\text{m}^3$  and  $4.84 \times 10^{23}/\text{m}^3$  for porphyrins and composites, respectively.

As for the input electric field, we choose a hyperbolic secant shape incident pulse

$$E(z, t=0) = F_0 \text{sech} \left[ 1.76(z/c + z_0/c) / \tau_p \right] \cos \left[ \omega(z + z_0)/c \right] \quad (12)$$

with the peak amplitude  $F_0$  which has a relationship with field intensity of  $I(t) = \frac{c\epsilon_0 |E_0(t)|^2}{2}$ . where  $\tau_p$  is the full width at half maximum (FWHM) of the pulse intensity profile,  $\omega$  is the carrier wave frequency of the incident pulse  $\omega = 2\pi c/\lambda$ . In order to match the experimental results, the laser parameters are set to  $\tau_p = 30$  ps,  $\lambda = 352$  nm, The choice of  $Z_0$  ensures that the pulse penetrates negligibly into the medium when  $t=0$ .