

## Mass Transport/Diffusion and Surface Reaction Process with Lattice Boltzmann

Giuseppe De Prisco<sup>1,2,\*</sup> and Xiaowen Shan<sup>1</sup>

<sup>1</sup> Exa Corporation, 55 Network Drive, Burlington, Massachusetts 01773, USA.

<sup>2</sup> Ingrain Inc, 3733 Westheimer Road, Houston, Texas 77027, USA.

Received 2 October 2009; Accepted (in revised version) 24 December 2010

Available online 18 February 2011

---

**Abstract.** Multi-component flow with chemical reactions is a common problem in different industrial applications: the mixing chamber of a reaction injection molding (RIM) machine; the dynamics of diesel soot particles interacting with a porous-ceramic particulate filter; reactive transport in porous media; bio-chemical processes involving enzyme-catalyzed kinetics. In all these cases, mass diffusion/convection and wall or volume chemical interactions among components play an important role. In the present paper we underline the importance of diffusion/convection/reaction mechanisms in bio-chemical processes using the Lattice Boltzmann (LB) technique. The bio-application where we studied diffusion/convection/reaction mechanisms is the quorum-sensing pathway for the bio-synthesis of the AI-2, a molecule that allows the bacteria to launch a coordinated attack on a host immune system (see [9, 10] for more details of the bio-application). The overall goal is to create a micro-device to screen potential drugs that inhibit AI-2 bio-synthesis. The Michaelis-Menten saturation kinetic model is implemented at the reactive surface and the results are shown in terms of two dimensionless numbers: Damkohler ( $Da$ ) and Peclet ( $Pe$ ) number. For high  $Pe$  number a small conversion of reactants into products is obtained at the reactive surface, but the overall flux of products is high; moreover, a fast saturation of the conversion of reactants to products is obtained for high  $Da$  numbers. The trade-off for setting the  $Pe$  and  $Da$  numbers depends on the specific application and the technologies used in the micro-device (e.g., sensitivity of the detector, cost of reactants).

**AMS subject classifications:** 76P05, 76R05, 76R50, 74F25, 92C45

**PACS:** 05.10.-a, 05.20.Dd, 47.11.Qr, 47.63.mf

**Key words:** Lattice Boltzmann, multi-component, diffusion-reaction.

---

\*Corresponding author. *Email addresses:* deprisco@ingrainrocks.com (G. De Prisco), xiaowen@exa.com (X. Shan)

## 1 Introduction

Bio-sensors and bio-chips are one of the most useful and challenging application based on microfluidic devices for different kinds of problems like DNA analysis, protein separation, antibiotics screening [9, 10]. Using of microdevices is ideal for parallel and automatic drugs screening, and it allows using small volume of expensive reagents. The bio-application that we are focusing on in this paper, in order to study diffusion/convection/reaction mechanisms using Lattice Boltzmann technique, is the quorum-sensing pathway for the bio-synthesis of the AI-2, a molecule that allows the bacteria launching a coordinate attack on a host immune system. The overall goal is to create and to optimize a microdevice to screen potential drugs that inhibit the AI-2 bio-synthesis (see [9, 10] for more details).

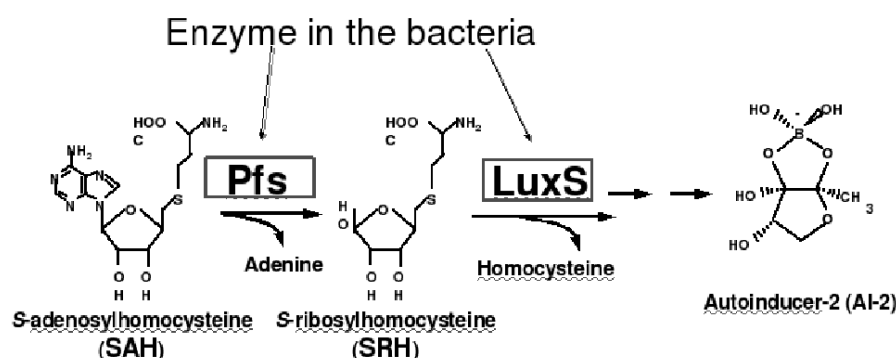


Figure 1: Schematic representation of the quorum sensing pathway (figure from [9, 10]): the complex molecular SAH reacts with the enzyme Pfs giving adenine and SRH as product. The SRH reacts with the enzyme LuxS giving the by-product homocysteine and the autoinducer-2 (AI-2) (see [9, 10] for more details).

The quorum sensing pathway involve two kinds of enzymes: either the Pfs or LuxS (see Fig. 1). It is clear from the scheme in Fig. 1 that one mole of SAH that reacts with the enzyme Pfs gives one mole of adenine and one mole of SRH. The by-product adenine is not involved in the successive steps of the reaction, so a common simplification is to consider a reaction where one mole of SAH produces one mole of SRH. A microdevice that can mimic the quorum sensing pathway is a microchannel with two patches on the bottom surface. The enzymes Pfs and Luxs are attached on the surface of the patches with a fixed superficial concentration so that the two patches can be considered as reactive surfaces: when a molecule of a reactant reaches the surface of the patch it can react with the attached enzyme to generate a molecule of product. At the inlet of the microchannel is introduced a potential inhibitors of the AI-2 whose efficiency is analyzed through the microdevice [9, 10]. A scheme of the microdevice is shown in Fig. 2; Fig. 3 shows the microchannel used in the experiment [9, 10]. In order to optimize the microdevice in terms of maximum sensitivity, minimal sample requirement and fastest screening times, the quorum-sensing pathway was simulated with a LB code, and the results were compared with available experimental analysis [9, 10]. The experimental analysis [9, 10] was con-